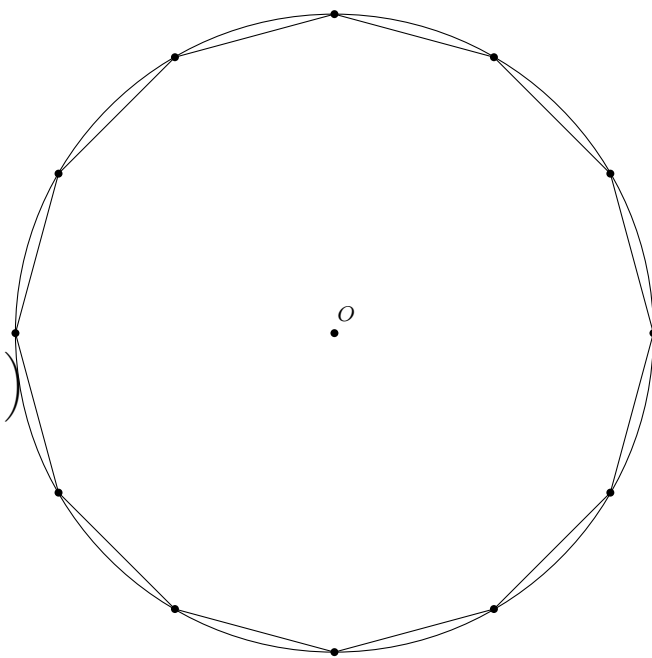


Write all responses on separate paper. Remember to organize your work clearly. You may *not* use your books, notes, or any calculator on this exam.

- (10 points) Use the substitution $x = \frac{3}{5} \tan \theta$ to simplify the expression $\frac{1}{x^2 \sqrt{25x^2 + 9}}$
- (10 points) Simplify the expression as much as possible: $\frac{\sin \phi}{1 - \cos \phi} + \frac{1 - \cos \phi}{\sin \phi}$
- (10 points) Find coefficients C and ϕ so that $2 \sin(4\theta) + 3 \cos(4\theta) = C \sin(4\theta + \arctan \phi)$.
- (15 points) Given that $\tan(\theta) = -3$ and θ is in quadrant II, find the following:
 - $\cos(2\theta)$.
 - $\sin(2\theta)$
 - $\tan(2\theta)$

- (10 points) Find the area of a regular polygon with twelve sides (a dodecagon) inscribed in the unit circle (radius = 1) as shown below. Do not approximate.



- (10 points) Use the addition identities to prove the product to sum identity,
$$\sin \alpha \sin \beta = \frac{1}{2} (\cos(\alpha - \beta) - \cos(\alpha + \beta))$$

- (10 points) Consider the point $\left(\cos \left(\frac{7\pi}{12} \right), \sin \left(\frac{7\pi}{12} \right) \right)$ on the unit circle.

- Use the addition identity on $\frac{7\pi}{12} = \frac{\pi}{3} + \frac{\pi}{4}$ to find simplified radical forms for the coordinates.
- Use the half angle formula on $\theta = \frac{7\pi}{6}$ to find different simplified radical forms for the coordinates.

- (9 points) Use the addition identities to express $\cos(5x)$ as quintic polynomial in $\cos(x)$.
- (16 points) Find all solutions in the interval $[0, 2\pi)$ for each equation.
 - $2 \cos(4\theta) + \sqrt{2} = 0$
 - $\cos^2(2\theta) - \cos(2\theta) - 1 = 0$