## Math 5 - Fall '16 - Test 1 Name (Print): Write all responses on separate paper. Show work for credit. No calculator/notes.

- 1. A bowling ball thrown by a bowler follows a parabolic trajectory given by the graph of the equation  $h(t) = 4 4 \left(t \frac{1}{2}\right)^2$ , where t is the time since ball was thrown and h(t) is the height of the ball above the ground at time t.
  - (a) What is the maximum height the bowling ball reaches?
  - (b) When does the bowling ball hit the ground?
- 2. Consider the polynomial function  $f(x) = x^3 \frac{5}{2}x^2 + \frac{1}{2}$ 
  - (a) Explain why this function does not satisfy the condition for the theorem on rational zeros. Write a function with the same zeros that does satisfy the condition.
  - (b) List all the possible rational zeros of the function.
  - (c) Write a complete factorization for the function.
  - (d) construct a careful graph of the function.0
- 3. Consider the polynomial function  $p(x) = 3x^4 + 10x^3 + 4x^2 5x 2$ .
  - (a) What does Descartes' rule of signs say about the number of positive and negative zeros of p?
  - (b) Use the Remainder Theorem to evaluate p(-4) and find q(x) so that p(x) = (x+4)q(x) + p(-4).
  - (c) Find P(1) and explain why there must be a zero in the interval (0,1)
  - (d) List all the possible rational zeros of p(x), according the theorem on rational zeros.
  - (e) Find all the zeros of p(x).
- 4. Write a formula for the polynomial function of degree 5 whose graph is shown:



5. Consider the rational function,  $r(x) = \frac{x^3 - 2x^2 - 3x}{x^2 - 4}$ 

- (a) What are the intercepts?
- (b) What asymptotes does it have?
- (c) Construct a table of values and a graph for the function.
- 6. Solve the inequality  $x \ge \frac{16-x}{2x+3}$
- 7. Find the domain of the function  $f(x) = \frac{1}{\sqrt{2x^3 + 7x^2 + 4x 4}}$