

Show all responses on separate paper. Show all work for credit.

1. Rewrite the equation  $-1 = \log_{16}(x+4)$  in equivalent exponential form, then solve for  $x$ . Finally, use a calculator to approximate  $x$  to the nearest hundredth.
2. Rewrite the equation  $2^{x-1} + 3 = 8$  in equivalent logarithmic form, then solve for  $x$ . Finally, use a calculator to approximate  $x$  to the nearest hundredth.
3. Rewrite the expression
  - a.  $\log\left(\frac{10}{3x^n}\right)$  without any exponentiation, multiplication or division.
  - b.  $\ln 1 + \frac{1}{2}\ln(e-x) - \ln(x)$  as a single logarithm.
4. Given  $f(x) = 2e^{x/3} - 8$ .
  - a. Find a formula for the inverse function,  $y = f^{-1}(x)$ .
  - b. Find the intercepts and asymptotes of  $f(x)$ .
  - c. Find the intercepts and asymptotes of  $f^{-1}(x)$ .
  - d. Sketch a graphing showing  $y = f(x)$  and  $y = f^{-1}(x)$  together and illustrating the symmetry through  $y = x$ .
5. Solve the equation for  $x$ .
  - a.  $8 + 4^{0.125x} = 24$
  - b.  $2^{1-x^2} = \frac{1}{8}$
  - c.  $1 + \log(17x + 104) = 2$
  - d.  $\log_3(8-x) + \log_3(x+4) = 3$
6. Suppose the Gorkon population on planet Xorda in April of 1999 was 1380, and it is estimated that the population will increase by 2% every 400 years.
  - a. Assuming a natural growth model for the zebra mussel, when will its population have grown to 2000?
  - b. By what percentage will the population grow in 1800 years?
7. If \$300 is invested at 3.65% annual interest rate compounded daily, how long will it take to reach a value of \$500?
8. Actinium has a half life of about  $7.04 \times 10^8$  years. How long will it take a 1 gram sample to decay to one milligram (one thousandth of a gram).
9. Find an exponential function (of the form  $f(x) = a \cdot b^x$ ) which passes through the points (0,3) and (2,5).