Exam 4 Prep: Chapters 7 & 8

- 1. Identify each algebraic statement as an expression or an equation. If the statement is an expression, perform the indicated operations and simplify. If the statement is an equation solve it.
 - (a) $\frac{7}{x^2+x-12} \frac{4}{x^2+4x} + \frac{3}{x^2-3x}$ (b) $\frac{3t-5}{4} \frac{t+1}{6} = \frac{t-2}{6}$ (c) $\frac{2x^2-8}{x^2-4x+4} \div \frac{3x^2-5x-2}{6x^2-10x-4}$
- 2. In the diagram below, $\triangle ABC$ is similar to $\triangle DEF$. That means that their corresponding sides are proportional.



- (a) Use the fact that the ratio of \overline{BC} to \overline{AB} is equal to the ratio of \overline{EF} to \overline{DE} to write an equation involving x.
- (b) Solve the equation to find all values of x that will work in the diagram and determine the length of \overline{DE} .
- 3. Recall that \sqrt{x} is defined for $x \ge 0$ as the positive number whose square is x.
 - (a) Simplify the expression $(\sqrt{x} \sqrt{81})^2$ for x = 16.
 - (b) Find all values of x so that $\sqrt{x^2 + 1} \sqrt{16} = 3$ and simplify these.
- 4. For each motion problem below, (i) Identify a variable, (ii) Fill in a table for distance D, rate R, and time T as shown at right, (iii) set up an equation and (iv) solve the equation to answer the question.

	Distance	Rate	Time
1st situation			
2nd situation			

- (a) A ferry goes 10 mph in still water. If it takes $\frac{5}{8}$ hour to travel the same distance upstream that it takes $\frac{5}{12}$ hour to travel downstream, what is the speed of the current?
- (b) Betty bicycles 12 mph faster when she goes 36 miles downhill than she does bicycling the same distance up the hill. If the trip up and down takes 8 hours, what is Betty's speed bicycling uphill?
- (c) There is a steady wind of 50 kph. If it takes a pilot 2 hours longer to fly a plane 8800 km against the wind than it does to fly 8100 km with the wind, what is the speed of the plane in still air?
- 5. Simplify each expression:

(a)
$$\sqrt{8} + \sqrt{32}$$
 (b) $\frac{1}{\sqrt{2}} + \frac{2}{\sqrt{3}}$ (c) $(1 - \sqrt{17})(1 + \sqrt{17})$ (d) $\frac{\sqrt{7} - \sqrt{5}}{\sqrt{7} + \sqrt{5}}$

- 6. Solve the following equations
 - (a) $\sqrt{4x+16} + 4 = 10$ (b) $\sqrt{2x+6} = x-1$
- 7. The legs of a right triangle have lengths $\sqrt[3]{2} 1$ and $\sqrt[3]{2} + 1$ Compute and simplify the length of the hypotenuse using Pythagoras' theorem.