

Math 05 – Spring 2011 – Take-home problems for Chapter 5 test

For each of these problems, show your own personal expression of the solution using a narrative style documenting each step in your derivation of the solution.

1. Suppose a conic section has a focus at $(0,0)$, eccentricity $e = 2$, and a vertex at $(9,0)$.
 - a. Find a standard polar function for the conic.
 - b. Find the standard rectangular equation for the conic.
 - c. Construct a careful graph of the conic showing key components.
 - d. Find parametric equations for the conic.
 - e. Pick a point P on the conic which is not a vertex and show that the ratio of the distance from that point to a focus to the distance from that point to the directrix is $\frac{d(P,F)}{d(P,\ell)} = e$

2. Suppose a conic section has a focus at $(0,0)$, eccentricity $e = \frac{1}{2}$, and a vertex at $(0,-8)$.
 - a. Find a standard polar function for the conic.
 - b. Find the standard rectangular equation for the conic.
 - c. Construct a careful graph of the conic showing key components.
 - d. Find parametric equations for the conic.
 - e. Pick a point P on the conic which is not a vertex and show that the ratio of the distance from that point to a focus to the distance from that point to the directrix is $\frac{d(P,F)}{d(P,\ell)} = e$