

Two Bodies

1. Write a program that will prompt the user to enter in the coordinates of two points in the Cartesian plane: (x_1, y_1) and (x_2, y_2) , which amounts to four `float` values. To do this, use `cout` to print the prompt, "Enter the coordinates x1, y1, x2, and y2:" to the console and then use `cin` to allow the user to enter these into variables named `x1, y1, x2, y2` (you will need to write appropriate variable declarations first). Then confirm the entries were successful by reporting to the user what they entered. That is, on a new line, print "You entered x1 = <the value>, y1 = <the value>, x2 = <the value>, y2 = <the value>". We will interpret these values as the coordinates in units of meters of two points (x_1, y_1) and (x_2, y_2) in the coordinate plane.
2. Extend problem 1 by computing the slope of the line through (x_1, y_1) and (x_2, y_2) and store this in a variable of type `double` named `slope`. Compute this slope as a decimal and print this to the console. Check that the slope is defined, and if it's not, write "A vertical line has no slope.", or words to that effect, and bail out of the program with `return 0`;
3. Use the `atan2()` function to compute the angle the line connecting the two points makes with the horizontal. You may need to `#include<cmath>` to get access to this function. Express this angle in both radians and degrees, being sure to indicate which is which.
4. Compute the components u_x and u_y of the unit vector $\hat{u} = \langle u_x, u_y \rangle$ from (x_1, y_1) to (x_2, y_2) . This is the vector of length 1 in that direction.
5. Prompt the user to enter the amount of mass (in kg) `m1` situated at (x_1, y_1) and the amount of mass (in kg) `m2` situated at (x_2, y_2) . Then use the formula $F = \frac{G \cdot m_1 \cdot m_2}{r^2}$ to compute the force (in Newtons) of gravitational attraction between these two masses.
6. Finally, compute and report the vector of force from m_1 to m_2 . This is done by multiplying a unit vector you computed in (4) by the scalar magnitude you computed in (5).

A typical run might look like this:

```
Enter the coordinates x1, y1, x2, and y2: 0 0 1 1
```

```
You entered points (0, 0) and (1, 1)
```

```
The slope of the line through these points is 1
```

```
This line makes the angle 0.785398 radians with the horizontal.
```

```
This is equivalent to 45 degrees.
```

```
A unit vector parallel to this line is (0.707107, 0.707107).
```

```
Enter the masses of the two objects at these points (in kg):
```

```
m1 = 1e6
```

```
m2 = 2e6
```

```
The force of gravitational attraction between these masses is the vector (47.1929, 47.1929) Newtons.
```

Include as a comment at the end of your code the results of a trial run or two like that shown above. Send your .cpp file to my email address with the format <your initials>_linear.cpp by Wednesday, February 12 at 9 am.